## Exercise 14.1

## Question 1:

A survey was conducted by a group of students as a part of their environment awareness programme, in which they collected the following data regarding the number of plants in 20 houses in a locality. Find the mean number of plants per house.

| Number of plants | $0-2$ | $2-4$ | $4-6$ | $6-8$ | $8-10$ | $10-12$ | $12-14$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of houses | 1 | 2 | 1 | 5 | 6 | 2 | 3 |

Which method did you use for finding the mean, and why?
Answer:
To find the class mark $\left(x_{i}\right)$ for each interval, the following relation is used.
Class mark $\left(x_{i}\right)=\frac{\text { Upper class limit }+ \text { Lower class limit }}{2}$
$x_{i}$ and $f_{i} x_{i}$ can be calculated as follows.

| Number of plants | Number of houses $\left(f_{i}\right)$ | $\boldsymbol{x}_{i}$ | $\boldsymbol{f}_{\boldsymbol{i}} \boldsymbol{x}_{\boldsymbol{i}}$ |
| :---: | :---: | :---: | :---: |
| 0-2 | 1 | 1 | $1 \times 1=1$ |
| $2-4$ | 2 | 3 | $2 \times 3=6$ |
| 4-6 | 1 | 5 | $1 \times 5=5$ |
| 6-8 | 5 | 7 | $5 \times 7=35$ |
| 8-10 | 6 | 9 | $6 \times 9=54$ |
| 10-12 | 2 | 11 | $2 \times 11=22$ |
| $12-14$ | 3 | 13 | $3 \times 13=39$ |


| Total | 20 |  | 162 |
| :---: | :---: | :---: | :---: |

From the table, it can be observed that
$\sum f_{i}=20$
$\sum f_{i} x_{i}=162$
Mean, $\bar{x}=\frac{\sum f_{i} x_{i}}{\sum f_{i}}$
$=\frac{162}{20}=8.1$
Therefore, mean number of plants per house is 8.1.
Here, direct method has been used as the values of class marks ( $x_{i}$ ) and $f_{i}$ are small.

## Question 2:

Consider the following distribution of daily wages of 50 worker of a factory.

| Daily wages (in <br> Rs) | $100-$ <br> 120 | $120-$ <br> 140 | $140-1$ <br> 60 | $160-$ <br> 180 | $180-$ <br> 200 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Number of <br> workers | 12 | 14 | 8 | 6 | 10 |

Find the mean daily wages of the workers of the factory by using an appropriate method.

Answer:
To find the class mark for each interval, the following relation is used.
$x_{i}=\frac{\text { Upper class limit }+ \text { Lower class limit }}{2}$
Class size $(h)$ of this data $=20$
Taking 150 as assured mean (a), $d_{i}, u_{i}$, and $f_{i} u_{i}$ can be calculated as follows.

## Page 2 of 49

| Daily wages <br> (in Rs) | Number of workers ( $\left.\boldsymbol{f}_{\boldsymbol{i}}\right)$ | $\boldsymbol{x}_{\boldsymbol{i}}$ | $\boldsymbol{d}_{\boldsymbol{i}}=\boldsymbol{x}_{\boldsymbol{i}}-\mathbf{1 5 0}$ | $\boldsymbol{u}_{\boldsymbol{i}}=\frac{\boldsymbol{d}_{\boldsymbol{i}}}{\mathbf{2 0}}$ | $\boldsymbol{f}_{\boldsymbol{i}} \boldsymbol{u}_{\boldsymbol{i}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $100-120$ | 12 | 110 | -40 | -2 | -24 |
| $120-140$ | 14 | 130 | -20 | -1 | -14 |
| $140-160$ | 8 | 170 | 20 | 1 | 6 |
| $160-180$ | 6 | 190 | 40 | 2 | 20 |
| $180-200$ | 50 |  |  | 0 | -12 |
| Total | 10 |  |  |  |  |

From the table, it can be observed that
$\sum f_{i}=50$
$\sum f_{i} u_{i}=-12$

$$
\begin{aligned}
\operatorname{Mean} \bar{x} & =a+\left(\frac{\sum f_{i} u_{i}}{\sum f_{i}}\right) h \\
& =150+\left(\frac{-12}{50}\right) 20 \\
& =150-\frac{24}{5} \\
& =150-4.8 \\
& =145.2
\end{aligned}
$$

Therefore, the mean daily wage of the workers of the factory is Rs 145.20 .

## Question 3:

The following distribution shows the daily pocket allowance of children of a locality.
The mean pocket allowance is Rs.18. Find the missing frequency $f$.

## Page 3 of 49

Class X
Chapter 14 - Statistics
Maths

| Daily pocket allowance <br> (in Rs) | $11-$ <br> 13 | $13-$ <br> 15 | 15 <br> -17 | $17-$ <br> 19 | $19-$ <br> 21 | $21-$ <br> 23 | $23-$ <br> 25 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of workers | 7 | 6 | 9 | 13 | $f$ | 5 | 4 |

Answer:
To find the class mark $\left(x_{i}\right)$ for each interval, the following relation is used.
$x_{i}=\frac{\text { Upper class limit }+ \text { Lower class limit }}{2}$
Given that, mean pocket allowance, $\bar{x}=$ Rs 18
Taking 18 as assured mean (a), $d_{i}$ and $f_{i} d_{i}$ are calculated as follows.

| Daily pocket allowance (in Rs) | Number of children $\boldsymbol{f}_{\boldsymbol{i}}$ | Class mark $\boldsymbol{x}_{\boldsymbol{i}}$ | $\begin{gathered} d_{i}=x_{i}- \\ 18 \end{gathered}$ | $\boldsymbol{f}_{i} \boldsymbol{d}_{\boldsymbol{i}}$ |
| :---: | :---: | :---: | :---: | :---: |
| $11-13$ | 7 | 12 | - 6 | $-42$ |
| $13-15$ | 6 | 14 | -4 | $-24$ |
| 15-17 | 9 | 16 | - 2 | $-18$ |
| 17-19 | 13 | 18 | 0 | 0 |
| 19-21 | $f$ | 20 | 2 | $2 f$ |
| 21-23 | 5 | 22 | 4 | 20 |
| 23-25 | 4 | 24 | 6 | 24 |
| Total | $\sum f_{i}=44+f$ |  |  | $\begin{gathered} 2 f- \\ 40 \end{gathered}$ |

From the table, we obtain

Class X
Chapter 14 - Statistics
Maths
$\sum f_{i}=44+f$
$\sum f_{i} u_{i}=2 f-40$
$\bar{x}=a+\frac{\sum f_{i} d_{i}}{\sum f_{i}}$
$18=18+\left(\frac{2 f-40}{44+f}\right)$
$0=\left(\frac{2 f-40}{44+f}\right)$
$2 f-40=0$
$2 f=40$
$f=20$
Hence, the missing frequency, $f$, is 20 .

## Question 4:

Thirty women were examined in a hospital by a doctor and the number of heart beats per minute were recorded and summarized as follows. Fine the mean heart beats per minute for these women, choosing a suitable method.

| Number of heart beats | $65-$ <br> 68 | $68-$ <br> 71 | 71 <br> -74 | $74-$ <br> 77 | $77-$ <br> 80 | $80-$ <br> 83 | $83-$ <br> 86 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of women | 2 | 4 | 3 | 8 | 7 | 4 | 2 |

Answer:
To find the class mark of each interval $\left(x_{i}\right)$, the following relation is used.
$x_{i}=\frac{\text { Upper class limit }+ \text { Lower class limit }}{2}$
Class size, $h$, of this data $=3$
Taking 75.5 as assumed mean (a), di, $u_{i}, f_{i} u_{i}$ are calculated as follows.

Class X

| Number of heart beats per minute | Number of women $\boldsymbol{f}_{i}$ | $\boldsymbol{X}_{\boldsymbol{i}}$ | $\begin{gathered} d_{i}=x_{i}- \\ 75.5 \end{gathered}$ | $u_{i}=\frac{d_{i}}{3}$ | $\boldsymbol{f}_{\boldsymbol{i}} \boldsymbol{u}_{\boldsymbol{i}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 65-68 | 2 | 66.5 | -9 | - 3 | $6$ |
| 68-71 | 4 | 69.5 | - 6 | - 2 | $8$ |
| 71-74 | 3 | 72.5 | - 3 | - 1 | $3$ |
| 74-77 | 8 | 75.5 | 0 | 0 | 0 |
| $77-80$ | 7 | 78.5 | 3 | 1 | 7 |
| 80-83 | 4 | 81.5 | 6 | 2 | 8 |
| 83-86 | 2 | 84.5 | 9 | 3 | 6 |
| Total | 30 |  |  |  | 4 |

From the table, we obtain

$$
\begin{aligned}
& \sum f i=30 \\
& \sum f_{i} u_{i}=4
\end{aligned}
$$

$$
\text { Mean } \begin{aligned}
\bar{x} & =a+\left(\frac{\sum f_{i} u_{i}}{\sum f_{i}}\right) \times h \\
& =75.5+\left(\frac{4}{30}\right) \times 3 \\
& =75.5+0.4=75.9
\end{aligned}
$$

Therefore, mean hear beats per minute for these women are 75.9 beats per minute.

## Page 6 of 49

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Class X
Chapter 14 - Statistics
Maths

## Question 5:

In a retail market, fruit vendors were selling mangoes kept in packing boxes. These boxes contained varying number of mangoes. The following was the distribution of mangoes according to the number of boxes.

| Number of mangoes | $50-52$ | $53-55$ | $56-58$ | $59-61$ | $62-64$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Number of boxes | 15 | 110 | 135 | 115 | 25 |

Find the mean number of mangoes kept in a packing box. Which method of finding the mean did you choose?

Answer:

| Number of mangoes | Number of boxes $\boldsymbol{f}_{\boldsymbol{i}}$ |
| :---: | :---: |
| $50-52$ | 15 |
| $53-55$ | 110 |
| $56-58$ | 135 |
| $59-61$ | 25 |
| $62-64$ |  |

It can be observed that class intervals are not continuous. There is a gap of 1
between two class intervals. Therefore, $\frac{1}{2}$ has to be added to the upper class limit and $\frac{1}{2}$ has to be subtracted from the lower class limit of each interval.
Class mark $\left(x_{i}\right)$ can be obtained by using the following relation.

## Page 7 of 49

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$$
x_{i}=\frac{\text { Upper class limit }+ \text { Lower class limit }}{2}
$$

Class size ( $h$ ) of this data $=3$
Taking 57 as assumed mean (a), $d_{i}, u_{i}, f_{i} u_{i}$ are calculated as follows.

| Class interval | $\boldsymbol{f}_{\boldsymbol{i}}$ | $\boldsymbol{x}_{\boldsymbol{i}}$ | $\boldsymbol{d}_{\boldsymbol{i}}=\boldsymbol{x}_{\boldsymbol{i}}-\mathbf{5 7}$ | $\boldsymbol{u}_{\boldsymbol{i}}=\frac{\boldsymbol{d}_{\boldsymbol{i}}}{\mathbf{3}}$ | $\boldsymbol{f}_{\boldsymbol{i}} \boldsymbol{u}_{\boldsymbol{i}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $49.5-52.5$ | 15 | 51 | -6 | -2 | -30 |
| $52.5-55.5$ | 110 | 54 | -3 | -1 | -110 |
| $55.5-58.5$ | 135 | 57 | 0 | 0 | 0 |
| $58.5-61.5$ | 115 | 60 | 3 | 1 | 115 |
| $61.5-64.5$ | 25 | 63 | 6 | 2 | 50 |
| Total | 400 |  |  |  | 25 |

It can be observed that
$\sum f_{i}=400$
$\sum f_{i} u_{j}=25$

$$
\text { Mean, } \begin{aligned}
\bar{x} & =a+\left(\frac{\sum f_{i} u_{i}}{\sum f_{i}}\right) \times h \\
& =57+\left(\frac{25}{400}\right) \times 3 \\
& =57+\frac{3}{16}=57+0.1875 \\
& =57.1875 \\
& =57.19
\end{aligned}
$$

Mean number of mangoes kept in a packing box is 57.19.

## Page 8 of 49

Class X

Step deviation method is used here as the values of $f_{i,} d_{i}$ are big and also, there is a common multiple between all $d_{i}$.

## Question 6:

The table below shows the daily expenditure on food of 25 households in a locality.

| Daily expenditure (in | $100-$ <br> 150 | $150-$ <br> 200 | $200-$ <br> 250 | $250-$ <br> 300 | $300-$ <br> 350 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Number of households | 4 | 5 | 12 | 2 | 2 |

Find the mean daily expenditure on food by a suitable method.
Answer:
To find the class mark $\left(x_{i}\right)$ for each interval, the following relation is used.
$x_{1}=\frac{\text { Upper class limit }+ \text { Lower class limit }}{2}$
Class size $=50$
Taking 225 as assumed mean (a), $d_{i}, u_{i}, f_{i} u_{i}$ are calculated as follows.

| Daily expenditure (in Rs) | $\boldsymbol{f}_{\boldsymbol{i}}$ | $\boldsymbol{x}_{\boldsymbol{i}}$ | $\boldsymbol{d}_{\boldsymbol{i}}=\boldsymbol{x}_{\boldsymbol{i}}-\mathbf{2 2 5}$ | $\boldsymbol{u}_{\boldsymbol{i}}=\frac{\boldsymbol{d}_{\boldsymbol{i}}}{\mathbf{5 0}}$ | $\boldsymbol{f}_{\boldsymbol{i}} \boldsymbol{u}_{\boldsymbol{i}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $100-150$ | 4 | 125 | -100 | -2 | -8 |
| $150-200$ | 5 | 175 | -50 | -1 | -5 |
| $200-250$ | 12 | 225 | 0 | 0 | 0 |
| $250-300$ | 2 | 325 | 100 | 2 | 4 |
| $300-350$ | 25 |  |  | 1 | 2 |
| Total |  |  |  | -7 |  |

From the table, we obtain

$$
\begin{aligned}
& \sum f_{i}=25 \\
& \sum f_{i} u_{i}=-7 \\
& \text { Mean, } \bar{x}
\end{aligned}=a+\left(\frac{\sum f_{j} u_{j}}{\sum f_{i}}\right) \times h \quad \begin{aligned}
& =225+\left(\frac{-7}{25}\right) \times(50) \\
& =225-14 \\
& =211
\end{aligned}
$$

Therefore, mean daily expenditure on food is Rs 211 .

## Question 7:

To find out the concentration of $\mathrm{SO}_{2}$ in the air (in parts per million, i.e., ppm ), the data was collected for 30 localities in a certain city and is presented below:

| concentration of $\mathbf{S O}_{\mathbf{2}}$ (in ppm) | Frequency |
| :---: | :---: |
| $0.00-0.04$ | 4 |
| $0.04-0.08$ | 9 |
| $0.08-0.12$ | 9 |
| $0.12-0.16$ | 2 |
| $0.16-0.20$ | 2 |
| $0.20-0.24$ |  |

Find the mean concentration of $\mathrm{SO}_{2}$ in the air.
Answer:
To find the class marks for each interval, the following relation is used.

Class X
$x_{i}=\frac{\text { Upper class limit }+ \text { Lower class limit }}{2}$
Class size of this data $=0.04$
Taking 0.14 as assumed mean (a), $d_{i}, u_{i}, f_{i} u_{i}$ are calculated as follows.

| Concentration of $\mathrm{SO}_{2}$ (in ppm) | Frequency $\boldsymbol{f}_{\boldsymbol{i}}$ | Class mark $\boldsymbol{X}_{i}$ | $\begin{gathered} d_{i}=x_{i}- \\ 0.14 \end{gathered}$ | $u_{i}=\frac{d_{i}}{0.04}$ | $\boldsymbol{f}_{i} u_{i}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0.00-0.04 | 4 | 0.02 | $-0.12$ | - 3 | $12$ |
| 0.04-0.08 | 9 | 0.06 | $-0.08$ | - 2 | $18$ |
| 0.08-0.12 | 9 | 0.10 | $-0.04$ | - 1 | -9 |
| $0.12-0.16$ | 2 | 0.14 | 0 | 0 | 0 |
| $0.16-0.20$ | 4 | 0.18 | 0.04 | 1 | 4 |
| 0.20-0.24 | 2 | 0.22 | 0.08 | 2 | 4 |
| Total | 30 |  |  |  | $31$ |

From the table, we obtain
$\sum f_{i}=30$
$\sum f_{i} u_{i}=-31$
Mean, $\bar{x}=a+\left(\frac{\sum f_{i} u_{i}}{\sum f_{i}}\right) \times h$

Class X

$$
\begin{aligned}
& =0.14+\left(\frac{-31}{30}\right)(0.04) \\
& =0.14-0.04133 \\
& =0.09867 \\
& \simeq 0.099 \mathrm{ppm}
\end{aligned}
$$

Therefore, mean concentration of $\mathrm{SO}_{2}$ in the air is 0.099 ppm .

## Question 8:

A class teacher has the following absentee record of 40 students of a class for the whole term. Find the mean number of days a student was absent.

| Number of days | $0-$ <br> 6 | $6-$ <br> 10 | $10-$ <br> 14 | $14-$ <br> 20 | $20-$ <br> 28 | $28-$ <br> 38 | $38-$ <br> 40 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of <br> students | 11 | 10 | 7 | 4 | 4 | 3 | 1 |

Answer:
To find the class mark of each interval, the following relation is used.
$x_{i}=\frac{\text { Upper class limit }+ \text { Lower class limit }}{2}$
Taking 17 as assumed mean (a), $d_{i}$ and $f_{i} d_{i}$ are calculated as follows.

| Number of days | Number of students <br> $\boldsymbol{f}_{\boldsymbol{i}}$ | $\boldsymbol{x}_{\boldsymbol{i}}$ | $\boldsymbol{d}_{\boldsymbol{i}}=\boldsymbol{x}_{\boldsymbol{i}}-\mathbf{1 7}$ | $\boldsymbol{f}_{\boldsymbol{i}} \boldsymbol{d}_{\boldsymbol{i}}$ |
| :---: | :---: | :---: | :---: | :---: |
| $0-6$ | 11 | 3 | -14 | -154 |
| $6-10$ | 10 | 8 | -9 | -90 |
| $10-14$ | 7 | 12 | -5 | -35 |


| $14-20$ | 4 | 17 | 0 | 0 |
| :---: | :---: | :---: | :---: | :---: |
| $20-28$ | 4 | 24 | 7 | 28 |
| $28-38$ | 3 | 33 | 16 | 48 |
| $38-40$ | 40 | 39 | 22 | 22 |
| Total | 1 |  |  | -181 |

From the table, we obtain
$\sum f_{i}=40$
$\sum f_{i} d_{i}=-181$

$$
\text { Mean, } \begin{aligned}
\bar{x} & =a+\left(\frac{\sum f_{i} d_{i}}{\sum f_{i}}\right) \\
& =17+\left(\frac{-181}{40}\right) \\
& =17-4.525 \\
& =12.475 \\
& \simeq 12.48
\end{aligned}
$$

Therefore, the mean number of days is 12.48 days for which a student was absent.

## Question 9:

The following table gives the literacy rate (in percentage) of 35 cities. Find the mean literacy rate.

| Literacy rate (in \%) | $45-55$ | $55-65$ | $65-75$ | $75-85$ | $85-95$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Number of cities | 3 | 10 | 11 | 8 | 3 |

Answer:
To find the class marks, the following relation is used.

Class X

$$
x_{i}=\frac{\text { Upper class limit }+ \text { Lower class limit }}{2}
$$

Class size $(h)$ for this data $=10$
Taking 70 as assumed mean (a), $d_{i}, u_{i}$, and $f_{i} u_{i}$ are calculated as follows.

| Literacy rate (in \%) | Number of cities <br> $\boldsymbol{f}_{\boldsymbol{i}}$ | $\boldsymbol{x}_{\boldsymbol{i}}$ | $\boldsymbol{d}_{\boldsymbol{i}}=\boldsymbol{x}_{\boldsymbol{i}}-\mathbf{7 0}$ | $\boldsymbol{u}_{\boldsymbol{i}}=\frac{\boldsymbol{d}_{\boldsymbol{i}}}{\mathbf{1 0}}$ | $\boldsymbol{f}_{\boldsymbol{i}} \boldsymbol{u}_{\boldsymbol{i}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $45-55$ | 3 | 50 | -20 | -2 | -6 |
| $55-65$ | 10 | 60 | -10 | -1 | -10 |
| $65-75$ | 11 | 70 | 0 | 0 | 0 |
| $75-85$ | 8 | 80 | 10 | 1 | 8 |
| $85-95$ | 3 | 90 | 20 | 2 | 6 |
| Total | 35 |  |  |  | -2 |

From the table, we obtain
$\sum f_{i}=35$
$\sum f_{i} u_{i}=-2$

$$
\text { Mean, } \begin{aligned}
\bar{x} & =a+\left(\frac{\sum f_{i} u_{i}}{\sum f_{i}}\right) \times h \\
& =70+\left(\frac{-2}{35}\right) \times(10) \\
& =70-\frac{20}{35} \\
& =70-\frac{4}{7} \\
& =70-0.57 \\
& =69.43
\end{aligned}
$$

Therefore, mean literacy rate is $69.43 \%$.

Exercise 14.2

## Question 1:

The following table shows the ages of the patients admitted in a hospital during a year:

| age (in years) | $5-15$ | $15-25$ | $25-35$ | $35-45$ | $45-55$ | $55-65$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of patients | 6 | 11 | 21 | 23 | 14 | 5 |

Find the mode and the mean of the data given above. Compare and interpret the two measures of central tendency.
Answer:
To find the class marks $\left(x_{i}\right)$, the following relation is used.

$$
x_{i}=\frac{\text { Upper class limit }+ \text { Lower class limit }}{2}
$$

Taking 30 as assumed mean (a), $d_{i}$ and $f_{i} d_{i}$ are calculated as follows.

| Age (in years) | Number of patients <br> $\boldsymbol{f}_{\boldsymbol{i}}$ | Class mark <br> $\boldsymbol{x}_{\boldsymbol{i}}$ | $\boldsymbol{d}_{\boldsymbol{i}}=\boldsymbol{x}_{\boldsymbol{i}}-\mathbf{3 0}$ | $\boldsymbol{f}_{\boldsymbol{i}} \boldsymbol{d}_{\boldsymbol{i}}$ |
| :---: | :---: | :---: | :---: | :---: |
| $5-15$ | 6 | 10 | -20 | -120 |
| $15-25$ | 11 | 20 | -10 | -110 |
| $25-35$ | 21 | 30 | 0 | 0 |
| $35-45$ | 23 | 50 | 20 | 280 |
| $45-55$ | 5 | 60 | 30 | 150 |
| $55-65$ | 80 |  |  | 430 |
| Total | 14 |  |  |  |

From the table, we obtain

Class X
Chapter 14 - Statistics
Maths
$\sum f_{i}=80$
$\sum f_{i} d_{i}=430$
Mean, $\bar{x}=a+\frac{\sum f_{i} d_{i}}{\sum f_{i}}$

$$
\begin{aligned}
& =30+\left(\frac{430}{80}\right) \\
& =30+5.375 \\
& =35.375 \\
& \simeq 35.38
\end{aligned}
$$

Mean of this data is 35.38 . It represents that on an average, the age of a patient admitted to hospital was 35.38 years.

It can be observed that the maximum class frequency is 23 belonging to class
interval 35-45.
Modal class $=35-45$
Lower limit (I) of modal class $=35$
Frequency $\left(f_{1}\right)$ of modal class $=23$
Class size $(h)=10$
Frequency $\left(f_{0}\right)$ of class preceding the modal class $=21$
Frequency $\left(f_{2}\right)$ of class succeeding the modal class $=14$
Mode $={ }^{l+\left(\frac{f_{1}-f_{0}}{2 f_{1}-f_{0}-f_{2}}\right) \times h}$
$=35+\left(\frac{23-21}{2(23)-21-14}\right) \times 10$
$=35+\left[\frac{2}{46-35}\right] \times 10$
$=35+\frac{20}{11}$
$=35+1.81$
$=36.8$

Class X
Chapter 14 - Statistics
Maths

Mode is 36.8 . It represents that the age of maximum number of patients admitted in hospital was 36.8 years.

## Question 2:

The following data gives the information on the observed lifetimes (in hours) of 225 electrical components:

| Lifetimes (in <br> hours) | $0-$ <br> 20 | $20-$ <br> 40 | $40-$ <br> 60 | $60-$ <br> 80 | $80-$ <br> 100 | $100-$ <br> 120 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 10 | 35 | 52 | 61 | 38 | 29 |

Determine the modal lifetimes of the components.
Answer:
From the data given above, it can be observed that the maximum class frequency is 61, belonging to class interval $60-80$.
Therefore, modal class $=60-80$
Lower class limit ( $/$ ) of modal class $=60$
Frequency $\left(f_{1}\right)$ of modal class $=61$
Frequency $\left(f_{0}\right)$ of class preceding the modal class $=52$
Frequency $\left(f_{2}\right)$ of class succeeding the modal class $=38$
Class size $(h)=20$

$$
\begin{aligned}
\text { Mode } & =l+\left(\frac{f_{1}-f_{0}}{2 f_{1}-f_{0}-f_{2}}\right) \times h \\
& =60+\left(\frac{61-52}{2(61)-52-38}\right)(20)
\end{aligned}
$$

$$
\begin{aligned}
& =60+\left(\frac{9}{122-90}\right)(20) \\
& =60+\left(\frac{9 \times 20}{32}\right) \\
& =60+\frac{90}{16}=60+5.625 \\
& =65.625
\end{aligned}
$$

Therefore, modal lifetime of electrical components is 65.625 hours.

## Question 3:

The following data gives the distribution of total monthly household expenditure of 200 families of a village. Find the modal monthly expenditure of the families. Also, find the mean monthly expenditure.

| Expenditure (in Rs) | Number of families |
| :---: | :---: |
| $1000-1500$ | 24 |
| $1500-2000$ | 40 |
| $2000-2500$ | 33 |
| $2500-3000$ | 28 |
| $3000-3500$ | 22 |
| $3500-4000$ | 16 |
| $4000-4500$ | 7 |
| $4500-5000$ |  |

Class X
Chapter 14 - Statistics
Maths

Answer:
It can be observed from the given data that the maximum class frequency is 40 ,
belonging to $1500-2000$ intervals.
Therefore, modal class $=1500-2000$
Lower limit ( $/$ ) of modal class $=1500$
Frequency $\left(f_{1}\right)$ of modal class $=40$
Frequency $\left(f_{0}\right)$ of class preceding modal class $=24$
Frequency $\left(f_{2}\right)$ of class succeeding modal class $=33$
Class size $(h)=500$

$$
\begin{aligned}
\text { Mode } & =l+\left(\frac{f_{1}-f_{0}}{2 f_{1}-f_{0}-f_{2}}\right) \times h \\
& =1500+\left(\frac{40-24}{2(40)-24-33}\right) \times 500 \\
& =1500+\left(\frac{16}{80-57}\right) \times 500 \\
& =1500+\frac{8000}{23} \\
& =1500+347.826 \\
& =1847.826=1847.83
\end{aligned}
$$

Therefore, modal monthly expenditure was Rs 1847.83.
To find the class mark, the following relation is used.
Class mark $=\frac{\text { Upper class limit }+ \text { Lower class limit }}{2}$
Class size $(h)$ of the given data $=500$
Taking 2750 as assumed mean (a), $d_{i}, u_{i}$, and $f_{i} u_{i}$ are calculated as follows.

| Expenditure (in <br> Rs) | Number of <br> families <br> $f_{i}$ | $x_{i}$ | $d_{i}=x_{i}-$ <br> 2750 | $u_{i}=\frac{d_{i}}{500}$ | $f_{i} u_{i}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |

## Page 19 of 49

Website: www.vidhyarjan.com

Class X
Chapter 14 - Statistics
Maths

| 1000-1500 | 24 | 1250 | - 1500 | - 3 | - 72 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1500-2000 | 40 | 1750 | - 1000 | $-2$ | $\begin{gathered} - \\ 80 \end{gathered}$ |
| 2000-2500 | 33 | 2250 | $-500$ | - 1 | $\begin{gathered} - \\ 33 \end{gathered}$ |
| 2500-3000 | 28 | 2750 | 0 | 0 | 0 |
| $3000-3500$ | 30 | 3250 | 500 | 1 | 30 |
| 3500-4000 | 22 | 3750 | 1000 | 2 | 44 |
| 4000-4500 | 16 | 4250 | 1500 | 3 | 48 |
| 4500-5000 | 7 | 4750 | 2000 | 4 | 28 |
| Total | 200 |  |  |  | - 35 |

From the table, we obtain
$\sum f_{i}=200$
$\sum f_{j} u_{j}=-35$
$\bar{x}($ mean $)=a+\left(\frac{\sum f_{i} u_{i}}{\sum f_{i}}\right) \times h$
$\bar{x}=2750+\left(\frac{-35}{200}\right) \times 500$
$=2750-87.5$
$=2662.5$
Therefore, mean monthly expenditure was Rs 2662.50.

## Question 4:

The following distribution gives the state-wise teacher-student ratio in higher secondary schools of India. Find the mode and mean of this data. Interpret the two measures.

| Number of students per teacher | Number of states/U.T |
| :---: | :---: |
| $15-20$ | 3 |
| $20-25$ | 8 |
| $25-30$ | 9 |
| $30-35$ | 30 |
| $35-40$ | 0 |
| $45-50$ | 0 |
| $50-55$ | 2 |

## Answer:

It can be observed from the given data that the maximum class frequency is 10
belonging to class interval $30-35$.
Therefore, modal class $=30-35$
Class size ( $h$ ) = 5
Lower limit ( $/$ ) of modal class $=30$
Frequency $\left(f_{1}\right)$ of modal class $=10$
Frequency $\left(f_{0}\right)$ of class preceding modal class $=9$
Frequency $\left(f_{2}\right)$ of class succeeding modal class $=3$

$$
\begin{aligned}
\text { Mode } & =l+\left(\frac{f_{1}-f_{0}}{2 f_{1}-f_{0}-f_{2}}\right) \times h \\
& =30+\left(\frac{10-9}{2(10)-9-3}\right) \times(5) \\
& =30+\left(\frac{1}{20-12}\right) 5 \\
& =30+\frac{5}{8}=30.625
\end{aligned}
$$

Mode $=30.6$
It represents that most of the states/U.T have a teacher-student ratio as 30.6 .
To find the class marks, the following relation is used.
Class mark $=\frac{\text { Upper class limit }+ \text { Lower class limit }}{2}$
Taking 32.5 as assumed mean (a), $d_{i}, u_{i}$, and $f_{i} u_{i}$ are calculated as follows.

| Number of students <br> per teacher | Number of <br> states/U.T <br> $\left(\boldsymbol{f}_{\boldsymbol{i}}\right)$ | $\boldsymbol{x}_{\boldsymbol{i}}$ | $\boldsymbol{d}_{\boldsymbol{i}}=\boldsymbol{x}_{\boldsymbol{i}}-$ <br> $\mathbf{3 2 . 5}$ | $\boldsymbol{u}_{\boldsymbol{i}}=\frac{\boldsymbol{d}_{\boldsymbol{i}}}{\mathbf{5}}$ | $\boldsymbol{f}_{\boldsymbol{i}} \boldsymbol{u}_{\boldsymbol{i}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $15-20$ | 3 | 17.5 | -15 | -3 | -9 |
| $20-25$ | 8 | 22.5 | -10 | -2 | - |
| $25-30$ | 9 | 27.5 | -5 | -1 | -9 |
| $30-35$ | 10 | 32.5 | 0 | 0 | 0 |
| $35-40$ | 3 | 37.5 | 5 | 1 | 3 |
| $40-45$ | 0 | 42.5 | 10 | 2 | 0 |

## Page 22 of 49

Website: www.vidhyarjan.com

| $45-50$ | 0 | 47.5 | 15 | 3 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $50-55$ | 2 | 52.5 | 20 | 4 | 8 |
| Total | 35 |  |  |  | - <br> 23 |

Mean, $\bar{x}=a+\left(\frac{\sum f_{i} u_{i}}{\sum f_{i}}\right) h$

$$
\begin{aligned}
& =32.5+\left(\frac{-23}{35}\right) \times 5 \\
& =32.5-\frac{23}{7}=32.5-3.28 \\
& =29.22
\end{aligned}
$$

Therefore, mean of the data is 29.2.
It represents that on an average, teacher-student ratio was 29.2.

## Question 5:

The given distribution shows the number of runs scored by some top batsmen of the world in one-day international cricket matches.

| Runs scored | Number of batsmen |
| :---: | :---: |
| $3000-4000$ | 4 |
| $4000-5000$ | 18 |
| $5000-6000$ | 9 |
| $6000-7000$ | 7 |


| $7000-8000$ | 6 |
| :---: | :---: |
| $8000-9000$ | 3 |
| $9000-10000$ | 1 |
| $10000-11000$ | 1 |

Find the mode of the data.
Answer:
From the given data, it can be observed that the maximum class frequency is 18 , belonging to class interval $4000-5000$.

Therefore, modal class $=4000-5000$
Lower limit ( $I$ ) of modal class $=4000$
Frequency $\left(f_{1}\right)$ of modal class $=18$
Frequency $\left(f_{0}\right)$ of class preceding modal class $=4$
Frequency $\left(f_{2}\right)$ of class succeeding modal class $=9$
Class size $(h)=1000$

$$
\begin{aligned}
\text { Mode } & =l+\left(\frac{f_{1}-f_{0}}{2 f_{1}-f_{0}-f_{2}}\right) \times h \\
& =4000+\left(\frac{18-4}{2(18)-4-9}\right) \times 1000 \\
& =4000+\left(\frac{14000}{23}\right) \\
& =4000+608.695 \\
& =4608.695
\end{aligned}
$$

Therefore, mode of the given data is 4608.7 runs

## Question 6:

A student noted the number of cars passing through a spot on a road for 100 periods each of 3 minutes and summarised it in the table given below. Find the mode of the data:

## Page 24 of 49

Website: www.vidhyarjan.com

Class X
Chapter 14 - Statistics
Maths

| Number of <br> cars | $0-$ <br> 10 | $10-$ <br> 20 | $20-$ <br> 30 | $30-$ <br> 40 | $40-$ <br> 50 | $50-$ <br> 60 | $60-$ <br> 70 | $70-$ <br> 80 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 7 | 14 | 13 | 12 | 20 | 11 | 15 | 8 |

Answer:
From the given data, it can be observed that the maximum class frequency is 20 , belonging to $40-50$ class intervals.

Therefore, modal class $=40-50$
Lower limit $(I)$ of modal class $=40$
Frequency $\left(f_{1}\right)$ of modal class $=20$
Frequency $\left(f_{0}\right)$ of class preceding modal class $=12$
Frequency $\left(f_{2}\right)$ of class succeeding modal class $=11$
Class size $=10$
Mode $=l+\left(\frac{f_{1}-f_{0}}{2 f_{1}-f_{0}-f_{2}}\right) \times h$
$=40+\left[\frac{20-12}{2(20)-12-11}\right] \times 10$
$=40+\left(\frac{80}{40-23}\right)$
$=40+\frac{80}{17}$
$=40+4.7$
$=44.7$
Therefore, mode of this data is 44.7 cars.

## Exercise 14.3

## Question 1:

The following frequency distribution gives the monthly consumption of electricity of 68 consumers of a locality. Find the median, mean and mode of the data and compare them.

| Monthly consumption (in units) | Number of consumers |
| :---: | :---: |
| $65-85$ | 4 |
| $85-105$ | 5 |
| $105-125$ | 13 |
| $125-145$ | 14 |
| $165-185$ | 4 |
| $185-205$ |  |

Answer:
To find the class marks, the following relation is used.
Class mark $=\frac{\text { Upper class limit }+ \text { Lower class limit }}{2}$
Taking 135 as assumed mean (a), $d_{i}, u_{i}, f_{i} u_{i}$ are calculated according to step deviation method as follows.

| Monthly <br> consumption (in <br> units) | Number of <br> consumers ( $\left.f_{i}\right)$ | $x_{i}$ class <br> mark | $d_{i}=x_{i}-$ <br> $\mathbf{1 3 5}$ | $\boldsymbol{u}_{i}=\frac{d_{i}}{\mathbf{2 0}}$ | $f_{i} \boldsymbol{u}_{i}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $65-85$ | 4 | 75 | -60 | -3 | - |

## Page 26 of 49

Website: www.vidhyarjan.com

|  |  |  |  |  | 12 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $85-105$ | 5 | 95 | -40 | -2 | - |
| $105-125$ | 13 | 115 | -20 | -1 | - |
| $125-145$ | 20 | 14 | 155 | 20 | 1 |
| $145-165$ | 8 | 175 | 40 | 2 | 16 |
| $165-185$ | 4 | 195 | 60 | 3 | 12 |
| $185-205$ | 68 |  |  | 0 | 0 |
| Total | 14 |  |  |  |  |

From the table, we obtain
$\sum f_{i} u_{i}=7$
$\sum f_{i}=68$
Class size $(h)=20$

$$
\text { Mean, } \begin{aligned}
\bar{x} & =a+\left(\frac{\sum f_{i} u_{i}}{\sum f_{i}}\right) \times h \\
& =135+\frac{7}{68} \times 20 \\
& =135+\frac{140}{68} \\
& =137.058
\end{aligned}
$$

From the table, it can be observed that the maximum class frequency is 20, belonging to class interval $125-145$.

Modal class = $125-145$

Lower limit ( $/$ ) of modal class $=125$
Class size $(h)=20$
Frequency $\left(f_{1}\right)$ of modal class $=20$
Frequency $\left(f_{0}\right)$ of class preceding modal class $=13$
Frequency $\left(f_{2}\right)$ of class succeeding the modal class $=14$
Mode $=l+\left(\frac{f_{1}-f_{0}}{2 f_{1}-f_{0}-f_{2}}\right) \times h$
$=125+\left[\frac{20-13}{2(20)-13-14}\right] \times 20$
$=125+\frac{7}{13} \times 20$
$=125+\frac{140}{13}=135.76$
To find the median of the given data, cumulative frequency is calculated as follows.

| Monthly consumption (in <br> units) | Number of <br> consumers | Cumulative <br> frequency |
| :---: | :---: | :---: |
| $65-85$ | 4 | 4 |
| $85-105$ | 5 | $4+5=9$ |
| $105-125$ | 13 | $9+13=22$ |
| $125-145$ | 14 | $22+20=42$ |
| $145-165$ | 8 | $56+8=64$ |
| $165-185$ | 4 | $64+4=68$ |
| $185-205$ | 20 |  |

From the table, we obtain
$n=68$
Cumulative frequency (cf) just greater than $\frac{n}{2}\left(\right.$ i.e., $\left.\frac{68}{2}=34\right)$ is 42 , belonging to interval 125 - 145.
Therefore, median class $=125-145$
Lower limit ( $/$ ) of median class $=125$
Class size $(h)=20$
Frequency ( $f$ ) of median class $=20$
Cumulative frequency ( $c f$ ) of class preceding median class $=22$

$$
\begin{aligned}
\text { Median } & =l+\left(\frac{\frac{n}{2}-c f}{f}\right) \times h \\
& =125+\left(\frac{34-22}{20}\right) \times 20 \\
& =125+12 \\
& =137
\end{aligned}
$$

Therefore, median, mode, mean of the given data is $137,135.76$, and 137.05 respectively.
The three measures are approximately the same in this case.

## Question 2:

If the median of the distribution is given below is 28.5, find the values of $x$ and $y$.

| Class interval | Frequency |
| :---: | :---: |
| $0-10$ | 5 |
| $10-20$ | $x$ |
| $20-30$ | 20 |

## Page 29 of 49

Website: www.vidhyarjan.com

Class X

| $30-40$ | 15 |
| :---: | :---: |
| $40-50$ | $y$ |
| $50-60$ | 5 |
| Total | 60 |

Answer:
The cumulative frequency for the given data is calculated as follows.

| Class interval | Frequency | Cumulative frequency |
| :---: | :---: | :---: |
| $0-10$ | 5 | 5 |
| $10-20$ | $x$ | $5+x$ |
| $20-30$ | 20 | $25+x$ |
| $30-40$ | 15 | $40+x$ |
| $40-50$ | $y$ | $40+x+y$ |
| $50-60$ | 60 |  |
| Total $(n)$ |  |  |

From the table, it can be observed that $n=60$
$45+x+y=60$
$x+y=15(1)$
Median of the data is given as 28.5 which lies in interval $20-30$.
Therefore, median class $=20-30$
Lower limit ( $/$ ) of median class $=20$
Cumulative frequency ( $c f$ ) of class preceding the median class $=5+x$
Frequency $(f)$ of median class $=20$

Class X
Chapter 14 - Statistics
Maths

Class size $(h)=10$
Median $=l+\left(\frac{\frac{n}{2}-c f}{f}\right) \times h$
$28.5=20+\left[\frac{\frac{60}{2}-(5+x)}{20}\right] \times 10$
$8.5=\left(\frac{25-x}{2}\right)$
$17=25-x$
$x=8$
From equation (1),
$8+y=15$
$y=7$
Hence, the values of $x$ and $y$ are 8 and 7 respectively
Question 3:
A life insurance agent found the following data for distribution of ages of 100 policy holders. Calculate the median age, if policies are given only to persons having age 18 years onwards but less than 60 year.

| Age (in years) | Number of policy holders |
| :---: | :---: |
| Below 20 | 2 |
| Below 25 | 6 |
| Below 30 | 24 |
| Below 35 | 45 |

Class X

| Below 40 | 78 |
| :---: | :---: |
| Below 45 | 89 |
| Below 50 | 92 |
| Below 55 | 98 |
| Below 60 | 100 |

Answer:
Here, class width is not the same. There is no requirement of adjusting the frequencies according to class intervals. The given frequency table is of less than type represented with upper class limits. The policies were given only to persons with age 18 years onwards but less than 60 years. Therefore, class intervals with their respective cumulative frequency can be defined as below.

| Age (in years) | Number of policy holders ( $\boldsymbol{f}_{\boldsymbol{i}}$ ) | Cumulative frequency (cf) |
| :---: | :---: | :---: |
| $18-20$ | 2 | 2 |
| $20-25$ | $6-2=4$ | 6 |
| $25-30$ | $24-6=18$ | 24 |
| $30-35$ | $78-45=33$ | 45 |
| $35-40$ | $89-78=11$ | 78 |
| $40-45$ | $92-89=3$ | 99 |
| $45-50$ | $98-92=6$ | 98 |
| $50-55$ | 75 |  |

## Page 32 of 49

Website: www.vidhyarjan.com

| $55-60$ | $100-98=2$ | 100 |
| :---: | :---: | :---: |
| Total $(n)$ |  |  |

From the table, it can be observed that $n=100$.
Cumulative frequency (cf) just greater than $\frac{n}{2}\left(\right.$ i.e., $\left.\frac{100}{2}=50\right)$ is 78 , belonging to interval 35-40.
Therefore, median class $=35-40$
Lower limit ( $/$ ) of median class $=35$
Class size ( $h$ ) $=5$
Frequency ( $f$ ) of median class $=33$
Cumulative frequency $(c f)$ of class preceding median class $=45$

$$
\begin{aligned}
\text { Median } & =l+\left(\frac{\frac{n}{2}-c f}{f}\right) \times h \\
& =35+\left(\frac{50-45}{33}\right) \times 5 \\
& =35+\frac{25}{33} \\
& =35.76
\end{aligned}
$$

Therefore, median age is 35.76 years.

## Question 4:

The lengths of 40 leaves of a plant are measured correct to the nearest millimeter, and the data obtained is represented in the following table:

| Length (in mm) | Number or leaves $\boldsymbol{f}_{\boldsymbol{i}}$ |
| :---: | :---: |
| $118-126$ | 3 |


| $127-135$ | 5 |
| :---: | :---: |
| $136-144$ | 9 |
| $145-153$ | 5 |
| $154-162$ | 4 |
| $163-171$ | 2 |
| $172-180$ |  |

Find the median length of the leaves.
(Hint: The data needs to be converted to continuous classes for finding the median, since the formula assumes continuous classes. The classes then change to 117.5 126.5, 126.5-135.5... 171.5-180.5)

Answer:
The given data does not have continuous class intervals. It can be observed that the difference between two class intervals is 1 . Therefore, $\frac{1}{2}=0.5$ has to be added and subtracted to upper class limits and lower class limits respectively.
Continuous class intervals with respective cumulative frequencies can be represented as follows.

| Length (in mm) | Number or leaves $\boldsymbol{f}_{\boldsymbol{i}}$ | Cumulative frequency |
| :---: | :---: | :---: |
| $117.5-126.5$ | 3 | 3 |
| $126.5-135.5$ | 5 | $3+5=8$ |
| $135.5-144.5$ | 9 | $8+9=17$ |
| $144.5-153.5$ | 12 | $17+12=29$ |

## Page 34 of 49

Website: www.vidhyarjan.com

| $153.5-162.5$ | 5 | $29+5=34$ |
| :---: | :---: | :---: |
| $162.5-171.5$ | 4 | $34+4=38$ |
| $171.5-180.5$ | 2 | $38+2=40$ |

From the table, it can be observed that the cumulative frequency just greater than
$\frac{n}{2}\left(\right.$ i.e., $\left.\frac{40}{2}=20\right)$
is 29, belonging to class interval 144.5 - 153.5.
Median class $=144.5-153.5$
Lower limit ( $/$ ) of median class $=144.5$
Class size $(h)=9$
Frequency ( $f$ ) of median class $=12$
Cumulative frequency ( $c f$ ) of class preceding median class $=17$

Median

$$
=l+\left(\frac{\frac{n}{2}-c f}{f}\right) \times h
$$

$=144.5+\left(\frac{20-17}{12}\right) \times 9$
$=144.5+\frac{9}{4}=146.75$
Therefore, median length of leaves is 146.75 mm .

## Question 5:

Find the following table gives the distribution of the life time of 400 neon lamps:

| Life time (in hours) | Number of lamps |
| :---: | :---: |
| $1500-2000$ | 14 |


| $2000-2500$ | 56 |
| :---: | :---: |
| $2500-3000$ | 60 |
| $3000-3500$ | 86 |
| $3500-4000$ | 62 |
| $4000-4500$ | 48 |
| $4500-5000$ |  |

Find the median life time of a lamp.
Answer:
Thecumulative frequencies with their respective class intervals are as follows.

| Life time | Number of lamps ( $\boldsymbol{f}_{\boldsymbol{i}}$ ) | Cumulative frequency |
| :---: | :---: | :---: |
| $1500-2000$ | 14 | 14 |
| $2000-2500$ | 56 | $14+56=70$ |
| $2500-3000$ | 60 | $70+60=130$ |
| $3000-3500$ | 86 | $216+74=290$ |
| $3500-4000$ | 62 | $350+62=352$ |
| $4000-4500$ | 48 |  |
| $4500-5000$ | 400 |  |
| Total $(n)$ |  |  |

Class X
Chapter 14 - Statistics
Maths

It can be observed that the cumulative frequency just greater than
$\frac{n}{2}\left(\text { i.e., } \frac{400}{2}=200\right)_{\text {is }}$ is 216, belonging to class interval $3000-3500$.

Median class $=3000-3500$
Lower limit ( $/$ ) of median class $=3000$
Frequency ( $f$ ) of median class $=86$
Cumulative frequency ( $c f$ ) of class preceding median class $=130$
Class size $(h)=500$

Median

$$
=l+\left(\frac{\frac{n}{2}-c f}{f}\right) \times h
$$

$=3000+\left(\frac{200-130}{86}\right) \times 500$
$=3000+\frac{70 \times 500}{86}$
$=3406.976$
Therefore, median life time of lamps is 3406.98 hours.

## Question 6:

100 surnames were randomly picked up from a local telephone directory and the frequency distribution of the number of letters in the English alphabets in the surnames was obtained as follows:

| Number of letters | $1-4$ | $4-7$ | $7-10$ | $10-13$ | $13-16$ | $16-19$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of surnames | 6 | 30 | 40 | 6 | 4 | 4 |

Determine the median number of letters in the surnames. Find the mean number of letters in the surnames? Also, find the modal size of the surnames.

Answer:

## Page 37 of 49

Website: www.vidhyarjan.com

The cumulative frequencies with their respective class intervals are as follows.

| Number of letters | Frequency ( $\left.\boldsymbol{f}_{\boldsymbol{i}}\right)$ | Cumulative frequency |
| :---: | :---: | :---: |
| $1-4$ | 6 | 6 |
| $4-7$ | 30 | $30+6=36$ |
| $7-10$ | 40 | $36+40=76$ |
| $10-13$ | 4 | $92+4=96$ |
| $13-16$ | 4 | $96+4=100$ |
| $16-19$ | 100 |  |
| Total $(n)$ |  |  |

It can be observed that the cumulative frequency just greater than $\frac{n}{2}\left(\right.$ i.e., $\left.\frac{100}{2}=50\right)$ is 76, belonging to class interval $7-10$.
Median class $=7-10$
Lower limit ( $/$ ) of median class $=7$
Cumulative frequency (cf) of class preceding median class $=36$
Frequency ( $f$ ) of median class $=40$
Class size $(h)=3$

Median

$$
=l+\left(\frac{\frac{n}{2}-c f}{f}\right) \times h
$$

$=7+\left(\frac{50-36}{40}\right) \times 3$
$=7+\frac{14 \times 3}{40}$
$=8.05$
To find the class marks of the given class intervals, the following relation is used.
Class mark $=\frac{\text { Upper class limit }+ \text { Lower class limit }}{2}$
Taking 11.5 as assumed mean (a), $d_{i}, u_{i}$, and $f_{i} u_{i}$ are calculated according to step deviation method as follows.

| Number of <br> letters | Number of <br> surnames <br> $\boldsymbol{f}_{\boldsymbol{i}}$ | $\boldsymbol{x}_{\boldsymbol{i}}$ | $\boldsymbol{d}_{\boldsymbol{i}}=\boldsymbol{x}_{\boldsymbol{i}}-$ <br> $\mathbf{1 1 . 5}$ | $\boldsymbol{u}_{i}=\frac{\boldsymbol{d}_{\boldsymbol{i}}}{\mathbf{3}}$ | $\boldsymbol{f}_{\boldsymbol{i}} \boldsymbol{u}_{\boldsymbol{i}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $1-4$ | 6 | 2.5 | -9 | -3 | -18 |
| $4-7$ | 30 | 5.5 | -6 | -2 | -60 |
| $7-10$ | 40 | 11.5 | 0 | -1 | -40 |
| $10-13$ | 4 | 14.5 | 3 | 1 | 4 |
| $13-16$ | 4 | 17.5 | 6 | 2 | 8 |
| $16-19$ | 100 |  |  | -3 | - |
| Total |  |  |  |  | 106 |

From the table, we obtain
$\Sigma f_{i} u_{i}=-106$
$\Sigma f_{i}=100$

Class X
Chapter 14 - Statistics
Maths
Mean, $\bar{x}=a+\left(\frac{\sum f_{i} u_{i}}{\sum f_{i}}\right) h$
$=11.5+\left(\frac{-106}{100}\right) \times 3$
$=11.5-3.18=8.32$
The data in the given table can be written as

| Number of letters | Frequency ( $\left.\boldsymbol{f}_{\boldsymbol{i}}\right)$ |
| :---: | :---: |
| $1-4$ | 6 |
| $4-7$ | 30 |
| $7-10$ | 40 |
| $10-13$ | 4 |
| $13-16$ | 4 |
| Total $(n)$ | 100 |

From the table, it can be observed that the maximum class frequency is 40 belonging to class interval 7-10.
Modal class $=7-10$
Lower limit (I) of modal class $=7$
Class size $(h)=3$
Frequency $\left(f_{1}\right)$ of modal class $=40$
Frequency $\left(f_{0}\right)$ of class preceding the modal class $=30$
Frequency $\left(f_{2}\right)$ of class succeeding the modal class $=16$

$$
\begin{aligned}
\text { Mode }= & l+\left(\frac{f_{1}-f_{0}}{2 f_{1}-f_{0}-f_{2}}\right) \times h \\
& =7+\left[\frac{40-30}{2(40)-30-16}\right] \times 3 \\
& =7+\frac{10}{34} \times 3 \\
& =7+\frac{30}{34}=7.88
\end{aligned}
$$

Therefore, median number and mean number of letters in surnames is 8.05 and 8.32 respectively while modal size of surnames is 7.88 .

## Question 7:

The distribution below gives the weights of 30 students of a class. Find the median weight of the students.

| Weight (in kg) | $40-$ <br> 45 | $45-$ <br> 50 | $50-$ <br> 55 | $55-$ <br> 60 | $60-$ <br> 65 | $65-$ <br> 70 | $70-$ <br> 75 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of <br> students | 2 | 3 | 8 | 6 | 6 | 3 | 2 |

Answer:
The cumulative frequencies with their respective class intervals are as follows.

| Weight (in kg) | Frequency (fi) | Cumulative frequency |
| :---: | :---: | :---: |
| $40-45$ | 2 | 2 |
| $45-50$ | 3 | $2+3=5$ |
| $50-55$ | 8 | $5+8=13$ |
| $55-60$ | 6 | $13+6=19$ |


| $60-65$ | 6 | $19+6=25$ |
| :---: | :---: | :---: |
| $65-70$ | 3 | $25+3=28$ |
| $70-75$ | 30 | $28+2=30$ |
| Total $(n)$ |  |  |

Cumulative frequency just greater than $\frac{n}{2}\left(\right.$ i.e., $\left.\frac{30}{2}=15\right)$ is 19 , belonging to class interval 55-60.

Median class $=55-60$
Lower limit ( $/$ ) of median class $=55$
Frequency ( $f$ ) of median class $=6$
Cumulative frequency ( $c f$ ) of median class $=13$
Class size $(h)=5$

Median

$$
=l+\left(\frac{\frac{n}{2}-c f}{f}\right) \times h
$$

$=55+\left(\frac{15-13}{6}\right) \times 5$
$=55+\frac{10}{6}$
$=56.67$
Therefore, median weight is 56.67 kg .

Exercise 14.4

## Question 1:

The following distribution gives the daily income of 50 workers of a factory.

| Daily income (in <br> Rs) | $100-$ <br> 120 | $120-$ <br> 140 | $140-$ <br> 160 | $160-$ <br> 180 | $180-$ <br> 200 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Number of workers | 12 | 14 | 8 | 6 | 10 |

Convert the distribution above to a less than type cumulative frequency distribution, and draw its ogive.

Answer:
The frequency distribution table of less than type is as follows.

| Daily income (in Rs) <br> (upper class limits) | Cumulative frequency |
| :---: | :---: |
| Less than 120 | 12 |
| Less than 140 | $12+14=26$ |
| Less than 160 | $26+8=34$ |
| Less than 180 | $40+10=50$ |
| Less than 200 |  |

Taking upper class limits of class intervals on $x$-axis and their respective frequencies on $y$-axis, its ogive can be drawn as follows.

## Page 43 of 49

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Class X


## Question 2:

During the medical check-up of 35 students of a class, their weights were recorded as follows:

| Weight (in kg) | Number of students |
| :---: | :---: |
| Less than 38 | 0 |
| Less than 40 | 3 |
| Less than 42 | 5 |
| Less than 44 | 9 |
| Less than 46 | 28 |
| Less than 48 | 32 |
| Less than 50 | 35 |
| Less than 52 |  |
| Draw a less than |  |

Draw a less than type ogive for the given data. Hence obtain the median weight from the graph verify the result by using the formula.

## Page 44 of 49

Website: www.vidhyarjan.com

Answer:
The given cumulative frequency distributions of less than type are

| Weight (in kg) <br> upper class limits | Number of students <br> (cumulative frequency) |
| :---: | :---: |
| Less than 38 | 0 |
| Less than 40 | 3 |
| Less than 42 | 5 |
| Less than 44 | 14 |
| Less than 46 | 28 |
| Less than 48 | 32 |
| Less than 50 | 35 |
| Less than 52 | 9 |

Taking upper class limits on $x$-axis and their respective cumulative frequencies on $y$ axis, its ogive can be drawn as follows.


Class X

So, $\frac{n}{2}=17.5$
Mark the point A whose ordinate is 17.5 and its $x$-coordinate is 46.5 . Therefore, median of this data is 46.5 .


It can be observed that the difference between two consecutive upper class limits is
2. The class marks with their respective frequencies are obtained as below.

| Weight (in kg) | Frequency (f) | Cumulative frequency |
| :---: | :---: | :---: |
| Less than 38 | 0 | 0 |
| $38-40$ | $3-0=3$ | 3 |
| $40-42$ | $5-3=2$ | 5 |
| $42-44$ | $9-5=4$ | 9 |
| $44-46$ | $14-9=5$ | 14 |
| $46-48$ | $28-14=14$ | 28 |
| $48-50$ | $32-28=4$ | 32 |


| $50-52$ | $35-32=3$ | 35 |
| :---: | :---: | :---: |
| Total (n) | 35 |  |

The cumulative frequency just greater than $\frac{n}{2}\left(\right.$ i.e., $\left.\frac{35}{2}=17.5\right)$ is 28 , belonging to class interval 46-48.

Median class $=46-48$
Lower class limit $(I)$ of median class $=46$
Frequency ( $f$ ) of median class $=14$
Cumulative frequency $(c f)$ of class preceding median class $=14$
Class size $(h)=2$

$$
\begin{aligned}
\text { Median } & =l+\left(\frac{\frac{n}{2}-c f}{f}\right) \times h \\
& =46+\left(\frac{17.5-14}{14}\right) \times 2 \\
& =46+\frac{3.5}{7} \\
& =46.5
\end{aligned}
$$

Therefore, median of this data is 46.5 .
Hence, the value of median is verified.

## Question 3:

The following table gives production yield per hectare of wheat of 100 farms of a village.

| Production yield (in <br> kg/ha) | $50-$ <br> 55 | $55-$ <br> 60 | $60-$ <br> 65 | $65-$ <br> 70 | $70-$ <br> 75 | $75-$ <br> 80 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |

## Page 47 of 49

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Change the distribution to a more than type distribution and draw ogive.
Answer:
The cumulative frequency distribution of more than type can be obtained as follows.

| Production yield <br> (lower class limits) | Cumulative frequency |
| :---: | :---: |
| more than or equal to 50 | 100 |
| more than or equal to 55 | $100-2=98$ |
| more than or equal to 60 | $98-8=90$ |
| more than or equal to 65 | $90-12=78$ |
| more than or equal to 70 | $78-24=54$ |
| more than or equal to 75 | $54-38=16$ |

Taking the lower class limits on $x$-axis and their respective cumulative frequencies on $y$-axis, its ogive can be obtained as follows.

Class X
Chapter 14 - Statistics
Maths


